Transportation-Distribution 941. Development Policy

Spring, 4(4-0) MTA 909, MTA 912.

Applications in theory, principles, and proceses developed in MTA 909 and MTA 912 to the design of research processes and reports in signficant transport and distribution problems.

Seminar in Micro Marketing 957. Spring. 4(4-0) MTA 911A.

Examines the current state of theory concerning the planning and implementation of marketing strategies and programs, and tries to identify where future research is needed and/or will be most useful to marketing and business manag-

Doctoral Dissertation Research 999.

Fall, Winter, Spring, Summer. Variable credit. Approval of department.

MATHEMATICS

MTH

College of Natural Science

One and one-half years of high school algebra and one year of geometry and a satisfactory score on the placement test are prerequisites for all courses in the Department of Mathematics which carry credit.

0813. Elements of Algebra

Fall, Winter, Spring, Summer. 0(3-0) [3(3-0) See page A-1 item 3.] Current enrollment in MTH 1033.

Fractions, decimals, real number properties, algorithms of arithmetic, simple factoring, simplifying algebraic expressions, parentheses, reciprocals, linear equations, integer exponents, applied problems, coordinate systems, graphing, solving equations by graphing.

Approved through Spring 1984.

0823. Intermediate Algebra

Fall, Winter, Spring, Summer. 0(2-0) [2(2-0) See page A-I item 3.] Current enrollment in MTH 1043, one year of high school algebra, satisfactory score on placement exam.

Properties of real numbers, polynomials, factoring, exponents, roots and radicals, first and second degree equations, linear inequalities, complex numbers, word problems, system of equations, operations on algebraic expressions, simplifying algebraic expressions. Approved through Spring 1984.

1033. Elements of Algebra

Fall, Winter, Spring, Summer. 2(2-0) Current enrollment in MTH 0813.

Fractions, decimals, real number properties, algorithms of arithmetic, simple factoring, simplifying algebraic expressions, parentheses, reciprocals, linear equations, integer exponents, applied problems, coordinate systems, graphing, solving equations by graphing.

Approved through Spring 1984.

1043. Intermediate Algebra

Fall, Winter, Spring, Summer. 3(3-0) Current enrollment in MTH 0823, one year of high school algebra, satisfactory score on placement exam.

Properties of real numbers, polynomials, factoring, exponents, roots and radicals, first and second degree equations, linear inequalities, complex numbers, word problems, system of equations, operations on algebraic expressions, simplifying algebraic expressions. Approved through Spring 1984.

108. College Algebra and Trigonometry I

Fall, Winter, Spring, Summer. 5(5-0) 1-1/2 high school units in algebra and satisfactory score on placement test, or MTH 0823; 1 high school unit in geometry. Not open to students with credit in MTH 111.

Number systems; variables; functions and relations; mathematical induction; exponents and radicals; elementary theory of equations; binomial theorem; determinants, matrices and systems of equations.

109. College Algebra and Trigonometry II

Fall, Winter, Spring, Summer. 5(5-0) MTH 108; not open to students with credit in MTH 111.

Continuation of MTH 108 plus trigonometry in-cluding definition of circular functions, angular measure, fundamental identities.

Finite Mathematics with Applications

Fall, Winter, Spring, Summer. 5(5-0) MTH 108 or MTH 111.

Elementary combinatorial analysis, binomial theorem, vectors and matrices, convex sets and linear programming, graph theory, applications to theory of games.

111. College Algebra with Trigonometry

Fall, Winter, Spring, Summer. 5(5-0) 1-1/2 years of high school algebra, I year of high school geometry, satisfactory score in algebra placement examination, trigonometry or MTH 102 or concurrently. Not open to students with credit in MTH 108 or MTH 109.

Sets and equations, simultaneous equations and matrices, vectors, inequalities, functions and relations, inverse functions, elementary theory of equations, trigonometric equations and identities, polar coordinates, parametric equations, straight line analytic geometry.

112. Calculus and Analytic Geometry

Fall, Winter, Spring, Summer. 5(5-0) MTH 109 or MTH 111.

The sequence MTH 112, MTH 113, MTH 214, MTH 215, is an integrated course in calculus and analytic geometry, covering derivatives, curve sketching, definite and indefinite integrals, area volume, transcendential functions, vector analysis, solid geometry, partial differentiation, multiple integrals, infinite series, power series.

Calculus and Analytic Geometry

Fall, Winter, Spring, Summer. 5(5-0) MTH 112.

A continuation of MTH 112.

Calculus I

Fall, Winter, Spring. 5(5-0) MTH 109 or MTH 111; not open to engineers, physical science or mathematics majors or to students with credit in MTH 112.

The first of a two-term course in primarily single variable calculus with and introduction to several variables for students who want only one or two terms of calculus.

123. Calculus II

Fall, Winter, Spring. 5(5-0) MTH 122, not open to engineers, physical science or mathematics majors or to students with credit in MTH 113.

The second of a two-term course in primarily single variable calculus with an introduction to several variables for students who want only one or two terms of calculus.

190. Freshman Mathematics Seminar

Winter, Spring. 3(3-0) Freshmen Mathematics majors; prior or concurrent calculus enrollment.

Intended to introduce mathematics majors to the type of mathematical reasoning and subject matter they can expect to encounter in advanced mathematics courses. Specific content will vary.

Mathematical Foundations for Elementary School Teachers

Fall, Winter, Spring, Summer. 4(4-0) 1-1/2 high school units in algebra and satisfactory score on placement test, or MTH 0823-1043; 1 high school unit in geometry. Open only to elementary education majors.

Fundamental concepts and processes of mathematics for prospective elementary school teachers.

204. Applied Mathematics in Elementary School

Winter, Spring. 4(4-0) MTH 201, elementary education majors.

Concepts and applications of algebra and geometry for prospective elementary teachers.

Calculus and Analytic Geometry

Fall, Winter, Spring, Summer. 4(4-0) MTH 113.

Continuation of MTH 113.

Calculus and Analytic Geometry 215.

Fall, Winter, Spring, Summer. 4(4-0) MTH 214.

Continuation of MTH 214.

Mathematics of Finance 216.

Winter. 3(3-0) MTH 108 or MTH 111.

Mathematical theory of interest with application to such topics as ordinary, due, and deferred annuities, amortization of debts; depreciation; capitalized cost; purchase price of bonds.

290. Special Topics in Mathematics

Fall, Winter, Spring. 1 to 5 credits. May reenroll for a maximum of 9 credits. Approval of department.

Individualized study adapted to the preparation and interests of the student. Topics studied will generally supplement and enrich the regular

302. Introduction to Combinatorics and Its Applications

Spring. 4(4-0) MTH 113.

Permutations combinations, the binomial and multinomial theorems, the principle of inclusion and exclusion, derangements, recurrence relations, Fibonacci sequences, generating functions, trees, graphs, chromatic polynomials, paths in networks.

309. Theory of Equations

Spring. 4(4-0) MTH 113 or approval of department.

Desirable for those preparing to teach mathematics in high schools. Mathematical induction, complex numbers, theorems in roots of polynomial equations, cyclotomic equations, ruler and compass constructions, solution of cubic and quartic equations, approximation to roots, theory of determinants, an introduction to ma-trices and some history of the theory of equations.

310. Differential Equations

Fall, Winter, Spring, Summer. 3(3-0) MTH 215 or concurrently.

First and second order equations; solutions in series, higher order equations; systems of differential equations, applications.

Courses

315. Concepts of Geometry I

Fall, Winter, Spring. 3(3-0) MTH 214 or approval of department.

Axiomatic structure of geometries including Euclidean, the classical non-Euclidean and projective geometries. Coordinate systems and geometric transformations.

316. Concepts of Geometry II

Winter, Spring. 3(3-0) MTH 315.

Continuation of MTH 315.

324. Foundations of Analysis

Fall, Winter, Spring. 4(4-0) MTH 215.

Elementary set theory; functions, mappings, equivalence relations; sequences and series; Cauchy sequences; least upper bound; countability; connected and compact sets; Bolzano Weierstrass Theorem; continuity.

331. Theory of Numbers

Fall, Winter, Spring. 3(3-0) MTH 113 or approval of department.

Diophantine equations, congruences, quadratic residues, finite fields.

334. Theory of Matrices

Fall, Winter, Spring, Summer. 4(4-0) MTH 214 or approval of department.

Algebra of matrices, vector spaces, rank, inverses, determinants, systems of equations, quadratic forms, Hermitian matrices, similarity transformations, characteristic values, linear transformations.

337. Concepts of Algebra

Winter. 3(3-0) MTH 214 or approval of department.

Rings, integral domains, properties of integers, fields, groups, polynomials.

341. Initial and Boundary Value Problems

Winter, Spring. 4(4-0) MTH 310.

Introduction to partial differential equations and initial and boundary value problems; emphasis on the wave equation, LaPlace's equation and heat flow equations and their solutions by separation of variables.

351. Introduction to Numerical Analysis

Winter, Spring. 4(4-0) MTH 310 and knowledge of FORTRAN programming; students may not receive credit in both MTH 351 and MTH 451.

Introduction to numerical analysis; computer coding using a compiler language; approximation to roots of equations, interpolation, numerical quadrature, numerical solution of ordinary differential equations.

352. Introduction to Numerical Solutions of Partial Differential Equation

Fall. 4(4-0) MTH 351.

Numerical solutions of boundary value problems, both two point and in the plane. Iterative methods for matrix equations. Introduction to stability and error analysis.

381. Chemical Engineering Analysis

Fall, Spring. 3(3-0) Students may not receive credit in both CHE 381 and MTH 341. MTH 310. Interdepartmental with and administered by the Department of Chemical Engineering.

Formulation of ordinary and partial differential equations describing chemical systems. Boundary value problems, numerical methods, matrices and applications, to chemical engineering systems.

400H. Honors Work

Fall, Winter, Spring. 1 to 16 credits. MTH 215 or approval of department.

Individualized reading and study in mathematics for students of high intellectual promise.

401. Geometry for Teachers

Summer. 3(3-0) Approval of department; not applicable to major or minor requirements.

Topics in geometry for junior and senior high school teachers.

405. Mathematical Topics for Teachers

Fall, Winter, Spring, Summer. 3(3-0) May reenroll for a maximum of 12 credits. Approval of department; open only to teachers participating in teacher institutes or special extension courses.

406. Mathematical Modeling for Teachers

(350.) Spring. 3(3-0) MTH 215.

Mathematical topics covered include: binary, octal and hexidecimal arithmetic, Euclidean algorithm and prime number generators, root finding for polynomials, approximation of functions, difference equations, combinatorics and probability problems, topics from geometry, and mathematical modeling and simulation.

414. Differential and Analytic Geometry

Spring. 4(4-0) MTH 215 or approval of department.

Coordinate systems in Euclidean three-space. Basic configurations. Vectors and the geometry of n-space. Transformations. Elementary differential geometry of curves and surfaces.

420. Ordinary Differential Equations Spring, 4(4-0) MTH 310, MTH 334.

Existence and uniqueness theorems, linear systems, plane autonomous systems, introduction to stability theory, Lyapunov's second method, applications.

421. Vector and Tensor Analysis

Fall, Winter, Summer. 4(4-0) MTH 310, MTH 334 recommended.

Vector calculus, line and surface integrals, divergence and Stokes theorem, orthogonal coordinate systems, introduction to tensors; applications to the physical sciences.

422. Boundary Value Problems and Fourier Series

Fall, Winter, Spring. 4(4-0) MTH 310, MTH 424.

Power series solutions of ordinary differential equations, Fourier series and orthogonal functions, partial differential equations of second order.

423. Complex Variables

Winter, Spring. 4(4-0) MTH 310 or approval of department.

Analytic functions, integrals, power series, residues, poles, conformal mapping and applications.

424. Advanced Calculus

Fall, Winter, Spring, Summer. 4(4-0) MTH 215.

Limits and continuity, function of several variables, ordinary and partial derivatives; theory of integration; multiple, line and surface integrals; infinite series, improper integrals, Beta and Gamma functions and other topics.

425. Advanced Calculus

Winter, Spring. 3(3-0) MTH 334, MTH

424.

Continuation of MTH 424.

426. Advanced Calculus

Fall, Spring. 3(3-0) MTH 425.

Continuation of MTH 425.

427. Real Analysis I

Fall. 4(4-0) Approval of department.

Topology, limits and continuity in En, functions of bounded variation, Riemann integration, calculus of several variables, linear transformations and derivatives.

428. Real Analysis II

Winter, 4(4-0) MTH 427.

Continuation of MTH 427.

429. Real Analysis III

Spring. 4(4-0) MTH 428.

Continuation of MTH 428.

430. Introduction to Error-Correcting Codes

Winter. 3(3-0) MTH 334.

Block codes and maximum likelihood decoding; Galois fields; encoding and decoding linear codes, cyclic codes (using shift registers), burst-error-correcting codes, convolutional codes.

432. Abstract Algebra I

Fall, Winter. 4(4-0) MTH 215.

Introduction to the concepts of basic algebraic structures, namely: group, ring, integral domain, field polynomial ring, module, vector space, linear transformation, etc.

433. Abstract Algebra II

Winter, Spring. 4(4-0) MTH 432.

Continuation of MTH 432.

434. Abstract Algebra III

Spring. 4(4-0) MTH 433.

Continuation of MTH 433.

437. Theory of Numbers II

Spring. 3(3-0) MTH 331 or MTH 432 or approval of department.

Dirichlet series, distribution of primes, sums of squares, Pell's equation, continued fractions, Hurewicz Theorem.

50. Mathematical Programming

Fall of even-numbered years. 3(3-1) MTH 424 or concurrently, MTH 334, knowledge of FORTRAN programming.

Finite dimensional convexity, theorems of the alternative, LR factorization, simplex algorithm, quasi-Newton methods, nonlinear duality theory, dual algorithms.

451. Numerical Analysis I

Winter, Spring. 4(4-0) MTH 310, MTH 334, MTH 424 or approval of department. Students may not receive credit in both MTH 351 and MTH 451.

Numerical solution of linear and nonlinear algebraic equations and eigenvalue problems; curve fitting, interpolation theory; numerical integration; differentiation and solution of differential equations; algorithms and computer programming.

452. Numerical Analysis II Spring. 4(4-0) MTH 451.

Continuation of MTH 451.

461. Topology

Winter, Spring. 3(3-0) MTH 424.

Introduction to fundamental concepts in topology, to metric and topological spaces, connectedness, compactness, continuity and simple connectedness.

462. Combinatorial Topology

Spring. 3(3-0) MTH 461 or MTH 424.

Unicursal graphs, surface topology, classification of surfaces, elementary set-theoretic topology, complexes.

471. Mathematical Logic

Fall. 4(4-0) MTH 215 or approval of department.

Language of mathematics. Informal axiomatic method. Propositional logic, validity, axiom and rules of inference, introduction to algebra of sets. Predicate logic. Logic of identity.

480. Mathematics for Economists

Fall. 5(5-0) MTH 113, graduate status in either economics, agricultural economics or College of Business, or approval of department. Interdepartmental with the Department of Economics

Matrix algebra, determinants, quadratic forms, characteristic values. Partial derivatives, chain rule, Jacobian matrix, Taylor series, constrained optimization, linear differential equations. Mathematics introduced and developed using student's background in economics.

481. Selected Mathematical Ideas in Biology

Winter, Spring. 4(4-0) MTH 214 or MTH 123.

Matrix algebra, difference and differential equations, graphical and numerical methods, discrete and continous population models, compartmental analysis, enzyme kinetics, theory of chemostat, hormonal controls, diffusion processes, food chains, pollution problems.

490. Mathematical Problems

Fall, Winter, Spring. 1 to 4 credits. May reenroll for a maximum of 8 credits. Approval of department.

Individualized study adapted to the preparation and interests of the student.

800. Set Theory and Foundations of Mathematics

Spring. Summer. 4(4-0) MTH 424 or approval of department.

Axiomatic method; various formulations of the axiom of choice; cardinal and ordinal numbers.

804. Linear Algebra and Analysis I Fall. 3(3-0) MTH 334, MTH 424.

Linear and matrix algebra, Grassman algebra, differential and integral calculus in Rn, linear differential equations, differential forms, closed and exact forms, Stokes theorem and elements of differential manifolds.

805. Linear Algebra and Analysis II Winter. 3(3-0) MTH 804.

Continuation of MTH 804.

806. Linear Algebra and Analysis III Spring. 3(3-0) MTH 805.

Continuation of MTH 805.

811. Theory of Relativity

Winter of even-numbered years. 4(4-0)
MTH 816.

Physical bases of theory of relativity. Introduction to space-time of two and four dimensions, and to relativistic dynamics, hydrodynamics and electromagnetism. Relativistic effects in solar gravitation field.

812. Foundations of Geometry

Fall. 4(4-0) MTH 426 or approval of department.

Incidence, affine and projective geometries. Finite projective planes, block designs. Lattice representations, coordination. Transformations Erlangen program, classical geometries. Metric topology, programs of Blumenthal and Busmann.

813. Geometry of Linear Spaces Winter. 4(4-0) MTH 812.

Linear topological spaces, Banach spaces, locally convex spaces. Linear transformations and functionals, extension theorems, conjugate spaces, weak topologies. Convexity, Krien-Milman theorem. Minkowski spaces, Helly's theorem. Caratheodory's theorem. Extremal structure.

814. Introduction to Differential Geometry

Spring. 4(4-0) MTH 426 or approval of department.

Curves and surfaces in 3-space, curvature, torsion, Frenet formulas. Riemannian manifolds, Gauss and mean curvature, geodesics, theorem egregium, Gauss-Codazzi equations, Gauss-Bonnet and Hilbert theorems.

816. Tensor Calculus and Riemannian Geometry

Fall of odd-numbered years. 4(4-0) MTH 426.

Contravariant and covariant tensors, metric tensors, geodesics, Christoffel symbols, covariant differentiation, curvature, Ricci tensor, parallel propagation, relative tensors, extension, spaces with affine connection, Weyl spaces; applications to dynamics, hydrodynamics and electromagnetic radiation.

817. Theory of Linear Graphs I

Winter. 3(3-0) MTH 334, MTH 424, or approval of department.

Fundamental concepts of undirected and directed graphs, including connectivity, trees, blocks, partitions, isomorphism, Menger's theorem, line graphs, coverings, Kuratowski's theroem, chromatic numbers, incidence matrices, and automorphism groups.

818. Theory of Linear Graphs II

Spring of even-numbered years. 3(3-0) MTH 817.

Advanced topics in the theory of linear graphs and combinatorial analysis. Polya's theorem and its application to enumeration problems.

821. Topology and Analysis I

Fall. 3(3-0) MTH 426 or MTH 804 or MTH 804 or MTH 804 concurrently; or approval of department.

Set theory, Zorn's Lemma, topology of Rn and metric spaces, topological spaces, Lebesgue integration, Hilbert and Banach spaces, linear operators.

822. Topology and Analysis II Winter. 3(3-0) MTH 821.

Winter. 3(3-0) MTH 821 Continuation of MTH 821.

823. Topology and Analysis III

Spring. 3(3-0) MTH 822.

Continuation of MTH 822.

824. Real and Complex Analysis Fall. 3(3-0) MTH 426.

Topics in this course, MTH 825 and MTH 826 selected from following: the real number system, linear point sets, theory of limits; continuity and differentiability properties of functions of one or more variables; sequences and series of functions: Riemann, Lebesgue and Stieltjes integrals, implicit function theory; existence theorems for differential equations.

825. Real and Complex Analysis

Winter. 3(3-0) MTH 824.

Continuation of MTH 824.

826. Real and Complex Analysis Spring. 3(3-0) MTH 825.

Continuation of MTH 825.

830. Error-Correcting Codes Fall. 3(3-0) MTH 334.

Algebraic background; theory of linear and cyclic codes; advanced topics.

831. Applied Matrix Theory

Winter, Summer. 4(4-0) MTH 334, MTH 424 or approval of department.

Row echelon form, inner products, quadratic forms; Gram, Unitary and Hermitian matrices; Gram Schmidt process; orthotriangular factorization; least error, least effort problems; determinants, eigen values and eigen vectors, diagonalization methods, rank factorizations.

832. Symmetry Groups and Their Applications

Spring. 3(3-0) Matrix theory.

Elementary Group Theory, orthogonal and isometry groups; isometrices as translations, rotations; glide reflections, screw rotations; symbols for isometries, point and space groups, lattices, latice groups, Bravais lattices, crystals.

834. Algebra I

Fall. 3(3-0) Approval of department.

Elements of group theory, direct complement and chain decomposition, classification of groups; ring theory, integral domains, field theory, extensions, automorphisms. Galois theory: modules and vector spaces, Wedderburn structure theory, linear and multilinear algebra.

835. Algebra II

Winter. 3(3-0) MTH 834.

Continuation of MTH 834.

836. Algebra III

Spring. 3(3-0) MTH 835.

Continuation of MTH 835.

841. Boundary Value Problems I

Fall. Summer of even-numbered years. 3(3-0) MTH 422, MTH 423; MTH 334 recommended.

Linear spaces, Fourier series. Boundary value problems for ordinary and partial differential equations. Variational methods. Fredholm integral equations. Integral transform. Distribution theory.

842. Boundary Value Problems II

Winter. 3(3-0) MTH 841.

Continuation of MTH 841.

843. Boundary Value Problems III

Spring. 3(3-0) MTH 842. Continuation of MTH 842. Courses

844. Methods of Applied Analysis I Fall. 3(3-0) MTH 334, MTH 423, MTH

426

Linear transformations on finite and infinite dimensional spaces. Fredholm and Hilbert-Schmidt theory, orthogonal polynomials, differential operators, Green's functions, Fourier transforms and distributions.

845. Methods of Applied Analysis II Winter, 3(3-0) MTH 844.

Continuation of MTH 844.

846. Methods of Applied Analysis III Spring. 3(3-0) MTH 845.

Continuation of MTH 845.

847. Theory of Ordinary Differential Equations I

Fall. 3(3-0) MTH 426; matrix theory.

Existence theorems; uniqueness and continuation of solutions; dependence of solutions on a parameter; linear systems; phase plane analysis.

Theory of Ordinary Differential 848. Equations II

Winter. 3(3-0) MTH 847.

Continuation of MTH 847; oscillation theory, asymptotic behavior, Lyapunov stability, boundary value problems.

249 Theory of Ordinary Differential Equations III

Spring. 3(3-0) MTH 848; approval of department.

Advanced topics in ordinary differential equa-

851. Numerical Analysis I

Fall. 3(3-0) MTH 426; FORTRAN programming and matrix theory recommended.

Numerical methods for solving systems of linear equations with error analysis; linear programming, the simplex algorithm; numerical procedures for determining eigenvalues and eigenvectors of matrices. Emphasis on computer applications.

Numerical Analysis II 852.

Winter. 3(3-0) MTH 851.

Numerical methods with error analysis for: solutions of nonlinear algebraic equations; Lagrange and Hermite interpolation: finite differences; approximation theory, including least square and Chebyshev approximations.

853. Numerical Analysis III

Spring. 3(3-0) MTH 852.

Numerical methods with error analysis for: differentiation; quadrature including New Newton-Cotes and Gaussian-type; difference equations; solutions of ordinary differential equations using one-step and multi-step predictor-corrector methods.

Mathematics of Operations 854. Research I

Fall. 3(3-0) MTH 804 or concurrently.

An introduction to those aspects of convex sets and convex functions that are useful in applied mathematics, economics, and other areas together with applications to linear and nonlinear programming problems.

855. Mathematics of Operations Research II

Winter. 3(3-0) MTH 854, MTH 805 or concurrently.

Continuation of MTH 854. Fixed point theorems, including Fan-Kakutani—Kuhn-Tucker theorems, duality theorems in nonlinear programming. Lagrangian conditions for constrained optima. Frobenius-Perron theory of non-negative matrices. Application to Economics and Business.

856. **Mathematics of Operations** Research III

Spring. 3(3-0) MTH 806 or concur-

rently.

Classical problems of variational calculus. Allocation and optimal control problems. Necessary conditions. Infinite dimensional programming and duality theory. Sufficiency conditions. Generalized Lagrange multipliers. Saddle point theory. Dynamic programming.

857. Numerical Methods in Partial Differential Equations

Spring. 4(4-0) MTH 422, knowledge of matrices recommended. Knowledge of computer programming desirable.

Numerical methods for solving initial and boundary value problems of partial differential

861. General Topology I

 $Fall.\ 3 (3\text{-}0)\ Approval\ of\ department.$

An introductory course in the topology of point sets. Concepts studied include topological spaces, products, homotopy and isotopy, separation, compactness, connectedness and path connectedness, metrization and compactifica-

862. General Topology II

Winter, 3(3-0) MTH 861.

Continuation of MTH 861 dealing with identification topology, covering axioms, partitions of unity, K spaces, Baire-spaces and function spaces.

863. General Topology III Spring. 3(3-0) MTH 862.

Development of homotopy theory required for more advanced studies with applications to covering spaces and the fundamental group.

864. Differential Topology

Spring of odd-numbered years. 3(3-0) MTH 426, MTH 862.

Smooth manifolds and maps. Submanifolds and embeddings. Mappings and approximations. Smoothing of maps and manifolds. Manifolds with boundary.

870. Foundations of Mathematics I

Fall of even-numbered years. 3(3-0) MTH 424; MTH 471 recommended.

Axiomatic set theory. Operations on sets, relations and functions, axiom of choice, maximal principles, cardinal and ordinal numbers, generalized, continuum hypothesis, axiom of constructibility, inaccessible cardinals.

871. Foundations of Mathematics II

Winter of odd-numbered years. 3(3-0) MTH 870.

Problems in metamathematics. Topics include: axiomatic systems, predicate calculus, consistency, completeness, and independence results, model theoretics, decision procedures, Godel's incompleteness theorem, recursive functions.

872. Foundations of Mathematics III

Spring of odd-numbered years. 3(3-0) MTH 871.

Continuation of MTH 871.

Foundations of Applied 881. Mathematics I

Fall. 3(3-0) MTH 426 or MTH 423.

Introduction to the mathematical theory of classical applied mathematics; properties and postulates of various theories such as ideal fluids and linear elasticity; derivation of field equa-tions; formulation of initial and boundary value problems.

882. Foundations of Applied Mathematics II

Winter. 3(3-0) MTH 881.

Continuation of MTH 881.

883. Foundations of Applied Mathematics III

Spring, 3(3-0) MTH 882.

Continuation of MTH 882.

884. Fluid Dynamics I

Fall of even-numbered years. 3(3-0) MTH 426 or MTH 422 or approval of depart-

Derivation of the equations of fluid mechanics. Comparisons of formulations, techniques and results in the basic disciplines of potential, viscous and gas dynamic flows.

885. Fluid Dynamics II

Winter of odd-numbered years, 3(3-0) MTH 884.

Continuation of MTH 884.

886. Partial Differential Equations I Fall. 3(3-0) MTH 334, MTH 423, MTH

426.

Cauchy-Kowalewski theorem; classification, characteristics, normal forms: general theory of first order equations; potential theory.

887. Partial Differential Equations II Winter. 3(3-0) MTH 886.

Elliptic type equations; Green's Neumann's and Kernel functions; boundary value problems and integral equations, hyperbolic equations, geometry of characteristics, Riemann's functions.

888. Partial Differential Equations

Spring. 3(3-0) MTH 887.

Continuation of hyperbolic equations; application of functional analysis to existence theorems, theory of Leray and Schauder.

890. Reading in Mathematics

Fall, Winter, Spring, Summer. 1 to 6 credits. May reenroll for a maximum of 36 credits. Approval of department,

899. Master's Thesis Research

Fall, Winter, Spring, Summer. Variable credit. Approval of department.

Harmonic Analysis I

Fall of even-numbered years. 3(3-0) MTH 823, MTH 862 or approval of department.

Fourier series, mean and point-wise convergence. Fourier-Stieltjes series. Maximal functions and a.e. convergence. Conjugate Interpolation ofoperators. Hausdorff-Young Theorems.

924. Functional Analysis I

Fall of odd-numbered years. 3(3-0) MTH 823, MTH 862 or approval of department. Topological groups and topological vector spaces, metrizability, locally convex spaces, Hahn-Banach and Krein-Milman theorems, dual spaces, Banach spaces, Hilbert spaces, Banach algebras.

925. Functional Analysis II

Winter of even-numbered years. 3(3-0) MTH 924 or approval of department. Continuation of MTH 924.

Functional Analysis III

Spring of even-numbered years. 3(3-0) MTH 925.

Continuation of MTH 925.

Theory of Measure and Integration 927.

Spring. 3(3-0) MTH 822. Interdepartmental with the Department of Statistics and Probability.

Introduction to the theory of integration over abstract spaces. Topics include: measure spaces; measurable and integrable functions; modes of convergence, theorems of Egroff, Lusin, Riesz-Fisher, Lebesgue absolute continuity, and the Radon-Nikodym theroem; product measures and Fubini's theorem. Applications to some of the classical theories of inte-gration and summability.

928. Harmonic Analysis II

Winter of odd-numbered years. 3(3-0) MTH 920.

Fourier transforms on Rn and R. Tempered distribution, inversion formula, Plancherel Theorem, pseudo-measures, almost-periodic functions, spectral properties, Wiener Tauberian Theorem, Paley-Wiener Theorems.

929. Harmonic Analysis III

Spring of odd-numbered years. 3(3-0) MTH 928

Selected topics from Fourier analysis on compact groups, singular integrals, harmonic analysis in Rn, Hp theory in one and several variables or differentiation of integrals.

934. Advanced Group Theory I Fall. 3(3-0) MTH 836.

Permutation groups, characters, π-properties, automorphisms, lattices of subgroups, classes of infinite groups, linear groups, recent literature.

935. Advanced Group Theory II Winter. 3(3-0) MTH 934.

Continuation of MTH 934.

936. Advanced Group Theory III Spring. 3(3-0) MTH 935.

Continuation of MTH 935.

Fluid Dynamics III 948.

Spring of odd-numbered years. 3(3-0) MTH 885.

General theory of perfect fluids including mo-tion of incompressible fluids in two and three dimensions and applications to problems of wing profiles. Viscous and compressible fluids discussed briefly.

951. Approximation Theory I

Fall of odd-numbered years. 3(3-0) MTH 823 or approval of department.

Tchebycheff, approximation with polynomials, rational functions and general linear families; the Uncity problem; degree of approximation; Berstein Polynomials; Remes algorithm, uniform approximation with constraints.

952. Approximation Theory II

Winter of even-numbered years. 3(3-0) MTH 951.

Continuation of MTH 951. Generalized methods of measuring error: Approximation in Li, and Lp norms, least-square approximation and orthogonal functions; spline functions; approximation in normed linear spaces.

Approximation Theory III 953.

Spring of even-numbered years, 3(3-0) MTH 952.

Continuation of MTH 952.

964. Algebraic Topology I

Fall. 3(3-0) MTH 834, MTH 862.

Simplicial and singular homotopy theory, Eilenberg-Steenrod axioms, chain complexes, cell complexes, applications to Euclidean spaces.

965. Algebraic Topology II

Winter, 3(3-0) MTH 964.

Continuation of MTH 964 including category and functor theory, general coefficient and cohomology theory.

966. Algebraic Topology III Spring. 3(3-0) MTH 965.

Continuation of MTH 965 including homology groups of products. Eilenberg-Zilber theorems, cohomology products, differential topology.

991. Advanced Topics in Geometry

Fall, Winter, Spring, Summer. 1 to 6 credits. May reenroll for a maximum of 36 credits. Approval of department.

992. Advanced Topics in Analysis

Fall, Winter, Spring, Summer. 1 to 6 credits. May reenroll for a maximum of 36 credits. Approval of department.

993. Advanced Topics in Algebra

Fall, Winter, Spring, Summer. 1 to 6 credits. May reenroll for a maximum of 36 credits. Approval of department.

Structure of rings and algebras, Lie Algebras, Jordan algebras, advanced algebraic number theory, advanced matrix theory, and advanced topics in group theory, Lattice theory.

994. Advanced Topics in Applied Mathematics

Fall, Winter, Spring, Summer. 1 to 6 credits. May reenroll for a maximum of 36 credits. Approval of department.

Nonlinear differential equations, asymptotic theory in differential equations, existence theorem, diffraction theory, Wiener-Hopf techniques.

999. Doctoral Dissertation Research

Fall, Winter, Spring, Summer. Variable credit. Approval of department.

MECHANICAL **ENGINEERING**

ME

College of Engineering

The Science of Sound I: Rock, Bach and Oscillators (N) 201.

Winter. 4(4-0) Interdepartmental with and administered by Physics.

Production, propagation, detection of sounds. Voice, hearing, scales, timbre, musical instruments. Room acoustics. Electronic reproduction and synthesis of music. Demonstrations emphasized.

202. The Science of Sound II

Spring. 3(3-0) or 4(4-0) PHY 201. Interdepartmental with Physics.

Nature, generation, and propagation of sound. Acoustical phenomenon and measurements. Storage and manipulation of sound in numerical form. Music programming.

300. Technology and Utilization of Energu

Winter, 3(3-0) Initial course in any sequence of courses in the Department of Natural

Problems of energy technology and its impact: energy sources, conversions, waste and environmental effects, future outlook.

Thermal-Fluid Phenomena

Spring. 3(3-0) MMM 201, MTH 113.

Concepts and principles used to describe, predict, or explain thermal and fluid-flow phenomena. Constraints, approximations, engineering problem solving. Application to socio-technical questions.

Thermodynamics I 311.

Fall, Winter, Spring. 3(3-0) MTH 215 or concurrently.

Zeroth, first and second laws of thermodynamics. General energy equation. Process relations. Concepts of equilibrium, reversibility, and irreversibility. Applications of these to systems describable by two independent properties.

312. Thermodynamics II

Winter, Spring. 3(3-0) M E 311.

Continuation of M E 311. Gas and vapor relations, reactive and non-reactive mixtures. Thermodynamic principle as applied to gas and vapor power and refrigeration cycles for reciprocating and turbo machinery.

320. Kinematics of Machines I

Fall, Spring, Summer. 4(3-3) MMM 306 or concurrently.

Analysis of displacement, velocity, and acceleration in mechanical linkages; cam analysis and design; analysis of spur, helical, bevel, and worm gears, including planetary systems.

Fluid Mechanics I

Winter, Spring. 4(3-3) M E 311; M E 351 or concurrently; MMM 306.

Fluid statics; Bernoulli equation; nondeformable control volume applied to conservation of mass, momentum and energy; derivation of differential equations of continuity and momentum; similtude.

333. Fluid Mechanics II

Fall, Spring, Summer. 4(3-3) ME 332.

Fluid flow phenomena; laminar flow; turbulent flow, pipe flow, inviscid flows; boundary layers; external flow; an introduction to compressible

347. Thermosciences and Energy Systems Laboratory

Winter, Spring. 1(0-3) M E 312 or concurrently.

Properties of pure substances; first law energy balances and second law analyses applied to a pump, turbine, refrigerator and combustion process.

351. Mechanical Engineering Analysis

Fall, Winter, Spring, Summer. 4(4-0) CPS 120 or concurrently, MTH 310.

Application of analytical and numerical methods to the solution of problems encountered in mechanical engineering.